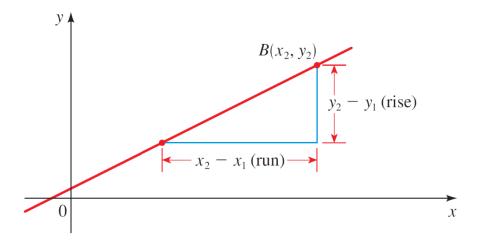
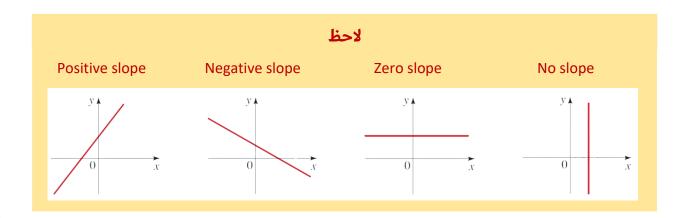


Section 1.10 - Lines

- The **slope** m of a line ميل الخط that passes through the points $A(x_1,y_1)$ and $B(x_2,y_2)$ is

$$m = \frac{\text{rise}}{\text{run}} = \frac{y_2 - y_1}{x_2 - x_1}$$





Example 1

Find the slope of the line that passes through the points P(2,1) and Q(8,5).

Solution

$$m = \frac{52-31}{22-22}$$

$$= \frac{5-1}{8-2} = \frac{4}{6} = \frac{2}{3}$$





Example 2

Find an equation of the line through the points (-1,2) and (3,-4).

Solution

$$M = \frac{92^{-10}}{22^{-12}} = \frac{-4^{-1}}{3^{-1}(-1)} = \frac{-6}{4} = -\frac{3}{2}$$

$$9 - 9 = M(x - x_1)$$

$$9 - 2 = -\frac{3}{2}(x - (-1))$$

$$9 - 2 = \frac{3}{2}(x - \frac{3}{2} + 2)$$

$$9 - \frac{3}{2}(x - \frac{3}{2} + 2)$$

$$9 = -\frac{3}{2}(x - \frac{3}{2} + 2)$$

Example 3

Find an equation of the line with slope 3 and y-intercept -2.

Solution

$$y = mx + b$$

 $y = 3x - 2$

لاحظ

- Point-slope form of the equation of a line:

$$y - y_1 = m(x - x_1)$$

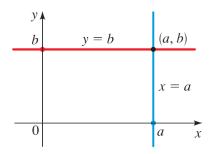
- Slope-intercept form of the equation of a line:

$$y = mx + b$$





- An equation of the vertical line through (a, b) is x = a.
- An equation of the horizontal line through (a, b) is y = b.



Example 4

Find an equation of the line through (1,3) with slope 0

Solution

- The graph of every linear equation

General equation of a line

$$Ax + By + C = 0$$

Ax + By + C = 0 (A, B not both zeros)

is a line. Its slope $m = -\frac{A}{B}$

Example 5

Find the slope of the line 2x - 3y - 12 = 0.

Solution

$$m = -\frac{L}{-5}$$

$$M = \frac{3}{3}$$





- Two lines are **parallel** متوازية if and only if they have the same slope $(m_1=m_2)$

Example 6

Find an equation of the line through the point (5,2) that is parallel to the line 4x + 6y + 5 = 0

Solution

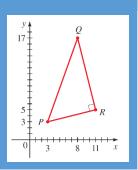
$$M_{2} = M_{1} = -\frac{4}{6} = -\frac{2}{3}$$
 $y-2 = -\frac{2}{3}(x-5)$
 $y-2 = -\frac{2}{3}x + \frac{10}{3}$
 $y = -\frac{2}{3}x + \frac{10}{3}$
 $y = -\frac{2}{3}x + \frac{10}{3}$
 $y = -\frac{2}{3}x + \frac{10}{3}$

- Two lines are **perpendicular** متعامدة if and only if their slopes are negative reciprocals:

$$m_2 = -\frac{1}{m_1}$$

Example 7

Show that the points P(3,3), Q(8,17), and R(11,5) are the vertices of a right triangle.



$$|M|_{PR} = \frac{5-3}{11-3} = \frac{2}{8} = \frac{1}{4}$$

$$M_{QR} = \frac{5-17}{11-8} = \frac{-12}{3} = -4$$

since mpr = - 1 then they







Problems

- Find an equation of the line with slope 2 and y-intercept -3.

- Find an equation of the line through (2,3) with slope 5







- Find an equation of the line through $(\mathbf{2},\mathbf{1})$ and $(\mathbf{1},\mathbf{6})$

- Find an equation of the line through $\left(2,-1\right)$ and slope undefined





- Find an equation of the line through $(\mathbf{1}, -\mathbf{6})$ and parallel to the line x + 2y = 6

- Find an equation of the line through $\left(-1,-2\right)$ and perpendcular to the line 2x + 5y + 8 = 0



